



# Cambridge International AS & A Level

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## MATHEMATICS

9709/31

Paper 3 Pure Mathematics 3

May/June 2025

1 hour 50 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

### INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages.



1 (a) Sketch the graph of  $y = |2x - 3|$ .

[1]

(b) Solve the inequality  $3x - 1 < |2x - 3|$ .

[2]

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Find  $q$  in terms of  $p$ .

[3]

[illegible]

- [illegible]

[illegible]

4

$$x = e^{\tan t}, \quad y = 3 \tan^2 t.$$

Find the equation of the tangent to the curve at the point  $(e, 3)$ . Give your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are exact. [6]

[illegible]



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[5]

[illegible]





6 It is given that  $z_1 = 3e^{\frac{1}{4}\pi i}$ ,  $z_2 = \frac{3}{2}e^{\frac{1}{6}\pi i}$  and  $\omega = 2e^{\frac{1}{2}\pi i}$ .

- (a) State the values of  $\omega z_1$  and  $\omega z_2$ . Give your answers in the form  $re^{i\theta}$ , where  $r > 0$  and  $-\pi < \theta \leq \pi$ . [2]

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- (b) On a sketch of an Argand diagram with origin  $O$ , show the points  $A$ ,  $B$ ,  $C$  and  $D$  representing the complex numbers  $z_1$ ,  $z_2$ ,  $\omega z_1$  and  $\omega z_2$  respectively. [2]

- (c) State the geometric effects of multiplying  $z_1$  and  $z_2$  by  $\omega$ . [2]

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- This image shows a full page of white paper with horizontal dashed lines, typical of primary school handwriting practice paper. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



[4]

[illegible]



- 8 With respect to the origin  $O$ , the points  $A$  and  $B$  have position vectors  $2\mathbf{i}+4\mathbf{k}$  and  $5\mathbf{i}+\mathbf{j}+6\mathbf{k}$  respectively. The line  $l_1$  passes through the points  $A$  and  $B$ .

- (a) Find a vector equation for the line  $l_1$ . [2]

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The line  $l_2$  has equation  $\mathbf{r} = 2\mathbf{i} + \mathbf{j} + 5\mathbf{k} + \mu(\mathbf{i} + 2\mathbf{j} + 3\mathbf{k})$ .

- (b) Show that  $l_1$  and  $l_2$  do **not** intersect. [4]

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(c) Find the acute angle between the directions of  $l_1$  and  $l_2$ . [3]

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(b) Verify by calculation that  $a$  lies between 2 and 2.1.

[2]

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(c) Use an iterative formula based on the equation in part (a) to determine  $a$  correct to 2 decimal places. Give the result of each iteration to 4 decimal places.

[3]

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- 10 (a) Find the quotient and remainder when  $x^3 + 5x^2 - 2x - 15$  is divided by  $x^2 - 3$ . [3]

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- (b) The variables  $x$  and  $y$  satisfy the differential equation

$$\frac{dy}{dx} = \frac{x^3 + 5x^2 - 2x - 15}{6y(x^2 - 3)}.$$

It is given that  $y = 2$  when  $x = 2$ .

Solve the differential equation to obtain an expression for  $y^2$  in terms of  $x$ . [5]

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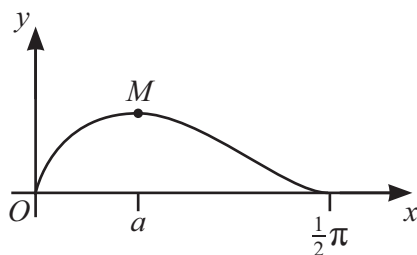
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The diagram shows the curve  $y = \cos x \sqrt{\sin 2x}$  for  $0 \leq x \leq \frac{1}{2}\pi$ . The curve has a maximum point at  $M$ , where  $x = a$ .

- (a) Find the exact value of  $a$ .

[6]

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- Find the exact volume of the solid generated.

[5]

[illegible]

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