



Cambridge International AS & A Level

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MATHEMATICS**9709/33**

Paper 3 Pure Mathematics 3

May/June 2025**1 hour 50 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has **20** pages. Any blank pages are indicated.



- 1 (a) Sketch the graph of $y = |3x - 2a|$, where a is a positive constant.

[1]

- (b) Hence or otherwise solve the inequality $|3x - 2a| < x + 5a$.

[3]

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[4]

This image shows a full page of a handwriting practice worksheet. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dotted lines, creating a series of uniform gaps for letter height. The entire page is otherwise blank, with no margins, text, or other markings.

[4]

This image shows a full page of white paper with horizontal dotted lines. The lines are evenly spaced and run across the width of the page, providing a guide for handwriting practice. There are no margins, text, or other markings on the page.



- 4 (a) It is given that $z_1 = r_1 e^{i\theta_1}$ and $z_2 = r_2 e^{i\theta_2}$.

Show that $(z_1 z_2)^* = z_1^* z_2^*$. [3]

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- (b) $z = 3e^{\frac{1}{4}\pi i}$ is a root of the equation $z^2 + bz + c = 0$, where b and c are real.

State the other root and hence find the values of b and c . [3]

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- [illegible]

(a) Express $f(x)$ in partial fractions.

[3]

[illegible]

[illegible]

[illegible]



[4]

[illegible]



- 9 With respect to the origin O , the points A , B and C have position vectors given by

$$\overrightarrow{OA} = \mathbf{i} + 2\mathbf{j}, \quad \overrightarrow{OB} = \mathbf{i} + 3\mathbf{j} - 2\mathbf{k} \quad \text{and} \quad \overrightarrow{OC} = 2\mathbf{i} - \mathbf{j} + 3\mathbf{k}.$$

The line l passes through B and C .

- (a) Find a vector equation for l .

[2]

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- (b) The point P is the foot of the perpendicular from A to l .

Find the position vector of P .

[4]

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(c) The point D is the reflection of A in l .

Find the position vector of D .

[2]

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It is given that $y = \frac{1}{12}\pi$ when $x = \frac{1}{2}\pi$.

$$\sin 4y \frac{dy}{dx} = x \sin 2y \sin 3x.$$

It is given that $y = \frac{1}{12}\pi$ when $x = \frac{1}{2}\pi$.

(a) Solve the differential equation, obtaining a relation between x and y .

[8]

[illegible]



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(b) Given that $0 < y < \frac{1}{2}\pi$, find the values of y when $x = 0$. [2]

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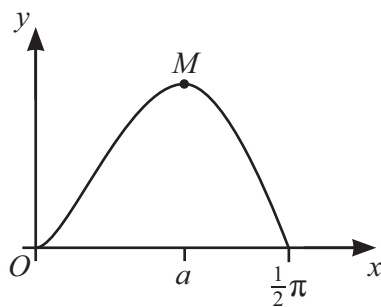
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The diagram shows the curve $y = \sqrt{x} \sin 2x$ for $0 \leq x \leq \frac{1}{2}\pi$. The curve has a maximum point at M , where $x = a$.

- (a) Show that $\tan 2a = -4a$ [4]

This image shows a full page of white paper with horizontal dashed lines, typical of primary school handwriting practice paper. The lines are evenly spaced and run across the entire width of the page. There are no margins, text, or other markings present.

- (b)** Show by calculation that $0.9 < a < 0.95$. [2]

[illegible]


$$x_{n+1} = \frac{1}{2} \left(\pi - \tan^{-1}(4x_n) \right)$$

[2]

[illegible]

[3]

[illegible]

[illegible]





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